## GCE 2005

January Series

ASSESSMENT and
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ALLIANCE

## Mark Scheme

## Mathematics

MPC2

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## Key to mark scheme and abbreviations used in marking

| M | mark is for method |  |  |
| :---: | :---: | :---: | :---: |
| m or dM | mark is dependent on one or more M marks and is for method |  |  |
| A | mark is dependent on M or m marks and is for accuracy |  |  |
| B | mark is independent of M or m marks and is for method and accuracy |  |  |
| E | mark is for explanation |  |  |
| $\checkmark$ or ft or F | follow through from previous incorrect result | MC | is-cop |
| CAO | correct answer only | MR | mis-read |
| CSO | correct solution only | RA | required accuracy |
| AWFW | anything which falls within | FW | further work |
| AWRT | anything which rounds to | ISW | ignore subsequent work |
| ACF | any correct form | FIW | from incorrect work |
| AG | answer given | BOD | given benefit of doubt |
| SC | special case | WR | work replaced by candidate |
| OE | OE | FB | formulae book |
| A2,1 | 2 or 1 (or 0) accuracy marks | NOS | not on scheme |
| $-x \mathrm{EE}$ | deduct $x$ marks for each error | G | graph |
| NMS | no method shown | c | candidate |
| PI | possibly implied | sf | significant figure(s) |
| SCA | substantially correct approach | dp | decimal place(s) |

MPC2


MPC2 (cont)

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline \begin{tabular}{l}
3(a)(i) \\
(ii) \\
(b) \\
(c)
\end{tabular} \& \[
\begin{aligned}
\& a+19 d=181 ; \\
\& a+4 d=46 \\
\& \Rightarrow 15 d=181-46 \\
\& \Rightarrow d=9 \\
\& a=10 \\
\& S_{20}=\frac{20}{2}[2 a+(20-1) d] \\
\& \ldots .=1910 \\
\& \sum_{n=1}^{50} u_{n}-\sum_{n=1}^{20} u_{n} \\
\& \ldots .=11525-" 1910 "=9615
\end{aligned}
\] \& \[
\begin{gathered}
\text { M1 } \\
\text { A1 } \\
\text { A1 } \\
\text { B1 } \\
\text { M1 } \\
\text { A1 } \\
\text { M1 } \\
\text { A1 }
\end{gathered}
\] \& \begin{tabular}{l}
\[
3
\] \\
1 \\
2 \\
2
\end{tabular} \& \begin{tabular}{l}
\(a+(n-1) d\) used; PI \\
AG (be convinced) \\
OE \\
OE \\
ft on 11525 - c's \(S_{20}\)
\end{tabular} \\
\hline \& Total \& \& 8 \& \\
\hline \begin{tabular}{l}
4(a) \\
(b) \\
(c) \\
(d)
\end{tabular} \& \[
\begin{aligned}
\& \sqrt{x}=x^{\frac{1}{2}} \\
\& \sqrt{x}(x-1)=x^{\frac{1}{2}} x-x^{\frac{1}{2}}=x^{\frac{3}{2}}-x^{\frac{1}{2}} \\
\& \int \sqrt{x}(x-1) \mathrm{d} x=\frac{x^{2.5}}{2.5}-\frac{x^{1.5}}{1.5}(+c) \\
\& \int_{1}^{2} \mathrm{~d} x=\left(\frac{2^{2.5}}{2.5}-\frac{2^{1.5}}{1.5}\right)-\left(\frac{1}{2.5}-\frac{1}{1.5}\right) \\
\& \ldots=\left(\frac{4 \sqrt{2}}{2.5}-\frac{2 \sqrt{2}}{1.5}\right)-\left(\frac{1}{2.5}-\frac{1}{1.5}\right) \\
\& \left(\frac{24 \sqrt{2}}{15}-\frac{20 \sqrt{2}}{15}\right)-\left(-\frac{4}{15}\right)=\mathrm{pr} . \mathrm{ans}
\end{aligned}
\] \& \begin{tabular}{l}
B1 \\
M1 \\
A1 \\
M1 \\
A1 \(\sqrt{ }\) \\
A1 \(\checkmark\) \\
M1 \\
m1 \\
A1
\end{tabular} \& 1
2

3
3

3 \& | Accept $k=0.5$ |
| :--- |
| Accept $p=1.5, q=0.5$ |
| Increases a power of $x$ by 1 |
| ft non-integer $p$ |
| ft non-integer $q$ |
| Limits; $F(2)-F(1)$ |
| Fractional powers to surds |
| CSO AG (be convinced) | <br>

\hline \& Total \& \& 9 \& <br>

\hline | 5(a) |
| :--- |
| (b)(i) |
| (ii) |
| (iii) |
| (iv) | \& \[

$$
\begin{aligned}
& \log _{a} x=\log _{a} 6^{3}-\log _{a} 8 \\
& \log _{a} x=\log _{a}\left(6^{3} \div 8\right) \\
& x=6^{3} \div 8=27
\end{aligned}
$$
\]

\[
$$
\begin{aligned}
& \log _{4} 1=0 \\
& \log _{4} 4=1 \\
& \log _{4} 2=0.5 \\
& \log _{4} 8=1.5
\end{aligned}
$$

\] \& | M1 |
| :--- |
| M1 |
| A1 |
| B1 |
| B1 |
| B1 |
| B1 | \& 3

4 \& | A law of logs used correctly |
| :--- |
| A different law of logs used correctly CSO AG (be convinced) $\begin{gather*} \underline{\text { ALT }} \log _{a} x=3 \log _{a} 6-3 \log _{\mathrm{a}} 2  \tag{M1}\\ \frac{1}{3} \log _{a} x=\log _{a} \frac{6}{2}  \tag{M1}\\ x^{\frac{1}{3}}=3 \Rightarrow x=27 \end{gather*}$ |
| (A1) CSO |
| SC in (b): For all four answers $1 / 4 ; 1 ; 1 / 2 ; 2$ give $0 / 4$; otherwise mark each independently. | <br>

\hline \& Total \& \& 7 \& <br>
\hline
\end{tabular}

MPC2 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 6(a)(i) | $\begin{aligned} & (2+x)^{3}= \\ & \quad\left(2^{3}\right)+3\left(2^{2}\right)(x)+3(2)\left(x^{2}\right)+\left(x^{3}\right) \\ & \ldots=8+12 x+6 x 2+x 3\left(^{*}\right) \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | 3 | Any valid method; must contain all components <br> Accept $a=12$ <br> Accept $b=6$ |
| (ii) | $(2-x)^{3}=8-12 x+6 x^{2}-x^{3}(* *)$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \checkmark \end{aligned}$ | 2 | Clear $x \rightarrow-x$ in (i) OE ft numerical $a$ and $b$ |
| (b) | $\begin{aligned} & (2+x)^{3}-(2-x)^{3}=\left({ }^{*}\right)-\left({ }^{* *}\right) \\ & \ldots \ldots=24 x+2 x^{3} . \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 2 | Subtracts the 2 expressions in (a) CSO AG (be convinced) |
| (c) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=24+6 x^{2}$ | M1 |  | A power of $x$ decreased by 1 |
|  | For st. pt. $24+6 x^{2}=0$ <br> Not possible since $24+6 x^{2}>0$ | $\begin{aligned} & \text { A1 } \\ & \text { E1 } \end{aligned}$ | 3 | Any valid explanation |
|  | Total |  | 10 |  |
| 7(a) | $A\left(0^{\circ}, 1\right)$ | B1 |  | Condone radians |
|  | $B\left(45^{\circ}, 0\right)$ | B1 |  | Condone ( $0.785,0$ ) or better. |
|  | $C\left(270^{\circ},-1\right)$ | B1, B1 | 4 | B1 for 270; B1 for -1 |
| (b) | Stretch (I) in $x$-direction (II) with a |  |  | More than one transformation is M0 |
|  | scale factor $\frac{1}{2}$ (III) | M1A1 | 2 | M1 for (I) and either (II) or (III) |
| (c) | $\cos ^{-1} 0.37=" 68.284 \ldots "(=\alpha)$ | M1 |  | $\left.\operatorname{Cos}^{-1} 0.37 \text { (PI eg by } 68.3 \text { or } 1.19\right)$ |
|  | $x=\frac{\alpha}{2}=34.1(42 .)^{\circ}$ | A1 |  | Condone $34.2^{\circ}, 34^{\circ}$ or 0.596 rads |
|  | $x=180-\frac{\alpha}{2}$ | m1 |  | OE eg $2 x=360-\alpha$ |
|  | $x=180+\frac{\alpha}{2} \text { and } x=180+180-\frac{\alpha}{2}$ | m1 |  | OE Need both ( OE for $2 x=$ ) with no extras (quadrants) within the given interval |
|  | $\begin{aligned} & 2 x=68.284 \ldots ; 291.715 \ldots ; \\ & 428.284 \ldots ; 651.715 \ldots \\ & x=\left(34.1^{\circ} ;\right) \end{aligned}$ |  |  |  |
|  | $145.9^{\circ} ; 214.1^{\circ} ; 325.9^{\circ}$ | A1 | 5 | Dep. on all three method marks. Must be in degrees |
|  | Total |  | 11 |  |

MPC2 (cont)


